

Efficient scheduling and routing for heterogeneous instant delivery orders: a multi-objective optimization approach with real-time adaptability

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Abstract

Efficient scheduling and routing of heterogeneous instant delivery orders pose significant challenges in achieving timely and cost-effective delivery operations. In this research, we propose a multi-objective optimization approach with real-time adaptability to address these challenges. We formulate a mathematical model that considers factors such as distance, importance of orders, capacity constraints, time windows, and cost per unit distance or time. The model aims to minimize the overall cost while optimizing the assignment of delivery orders to delivery agents and determining the corresponding routes. We present a numerical example to illustrate the application of the model and discuss the results obtained. The findings highlight the effectiveness of the proposed approach in achieving efficient scheduling and routing, leading to improved resource utilization, cost reduction, and enhanced customer satisfaction. This research contributes to the field of instant delivery services by providing a systematic framework that can be employed to optimize operations in real-world delivery scenarios.

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Introduction

There has been a significant increase in the demand for instant delivery services driven by the rise of e-commerce and the expectation for quick and convenient product delivery (Kayikci, 2019) (Weltevreden, 2008) (Cohen, 2018). Instant delivery services aim to provide fast and efficient delivery of various goods, such as food, groceries, and consumer products, directly to the customers' doorstep within a short time frame (Davis, 1993) (Ulmer & Thomas, 2018).

Managing the scheduling and routing of heterogeneous instant delivery orders poses significant challenges for delivery service providers (W. Li et al., 2021) (Sheng et al., 2015) (Snoeck et al., 2020). The complexity arises from several factors, including varying order characteristics (e.g., size, weight, perishability), customer locations, delivery agent availability, traffic conditions, and the need for real-time adaptability to handle dynamic changes in the delivery environment (Dorer & Calisti, 2005) (Berbeglia et al., 2010) (Bock, 2010) (Skobelev, 2015).

Delivery scheduling and routing were tackled using heuristic-based approaches that did not fully consider multiple conflicting objectives simultaneously (Mankowska et al., 2014) (Moons et al.,

2017)(Goodarzi et al., 2020)(Khalifehzadeh et al., 2017)(Mamashli et al., 2021)(Cafaro & Cerdá, 2010)(Zajac & Huber, 2021)(Ullrich, 2013). These approaches often focused on single objectives, such as minimizing distance or maximizing delivery agent utilization, leading to suboptimal solutions and inefficiencies in the delivery process(Zajac & Huber, 2021).

To address these challenges and improve the efficiency of instant delivery services, researchers have turned to multi-objective optimization techniques(He et al., 2018)(Zhang et al., 2017)(Hua et al., 2021)(Tirkolaei et al., 2020)(Tirkolaei et al., 2020)(Luo et al., 2021). Multi-objective optimization allows for the simultaneous optimization of multiple objectives(Aydemir-Karadag & Turkbey, 2013)(Yan & Li, 2013)(Banasik et al., 2017)(Deb & Deb, 2013), considering their trade-offs, and generating a set of Pareto-optimal solutions that represent the best compromise between conflicting objectives(Taboada & Coit, 2007).

The objectives in the context of instant delivery services can include minimizing delivery time, maximizing customer satisfaction(Ryu & Han, 2010)(Nguyen et al., 2019)(F. Li et al., 2021), reducing delivery costs, and ensuring fair workload distribution among delivery agents(Cleophas & Ehmke, 2014)(Prasetyo et al., 2021). Achieving these objectives requires an algorithmic approach that can handle the complexity of the problem, integrate real-time data updates, and provide flexibility to adapt to dynamic changes in the delivery environment(Sarma et al., 2006)(Zhou et al., 2009).

By developing a multi-objective optimization approach with real-time adaptability for scheduling and routing heterogeneous instant delivery orders, several benefits can be obtained(Ojstersek et al., 2020)(Pourmohammad-Zia et al., 2020)(S. Iqbal et al., 2015)(Ghannadpour et al., 2014)(Sheu, 2007). These include improved delivery efficiency, reduced delivery time, increased customer satisfaction, optimized resource allocation, and enhanced overall operational performance for delivery service providers(Poirier & Reiter, 1996)(Walters, 2008).

Multi-objective optimization for vehicle routing problem with time windows and multiple objectives by Liu et al. (2017): This study proposes a multi-objective optimization model for the vehicle routing problem with time windows, which shares similarities with the instant delivery scheduling and routing problem. The authors consider multiple objectives, including minimizing travel distance, minimizing waiting time, and maximizing customer satisfaction. They utilize a hybrid algorithm combining genetic algorithms and local search to generate optimal solutions.

Real-time adaptive vehicle routing for on-demand ride-sharing services by Zheng et al. (2019): Although focused on ride-sharing services, this research addresses the real-time adaptability aspect relevant to instant delivery scheduling and routing. The study proposes a real-time adaptive vehicle routing framework that considers real-time demand and traffic conditions. The authors develop an algorithm to dynamically adjust the routes based on incoming requests, cancellations, and traffic congestion.

Efficient pickup and delivery problem with time windows: A multi-objective evolutionary approach by Valdez-Fernandez et al. (2020): This research focuses on the pickup and delivery problem, which shares similarities with instant delivery scheduling and routing. The authors propose a multi-objective evolutionary algorithm to optimize multiple objectives, including minimizing travel time, maximizing customer satisfaction, and reducing costs. The algorithm incorporates real-time adaptability by allowing changes to the routes based on dynamic updates.

A multi-objective optimization model for dynamic pickup and delivery problems with time windows in E-commerce by Yuan et al. (2021): This study addresses the dynamic nature of pickup and delivery problems in the context of e-commerce, which is relevant to instant delivery scheduling and routing. The authors propose a multi-objective optimization model considering objectives such as minimizing total travel distance, maximizing customer satisfaction, and minimizing the number of unassigned orders. The model is designed to adapt to dynamic changes in order requests and traffic conditions.

Real-time optimization for large-scale ride-sharing systems with demand-supply matching by Wang et al. (2021): Although focused on ride-sharing systems, this research explores real-time optimization and matching in a large-scale setting, which can be applicable to instant delivery scheduling and routing. The authors propose a real-time optimization framework that considers demand-supply matching and adapts the matching process based on real-time updates.

Efficient scheduling and routing for heterogeneous instant delivery orders poses a complex optimization problem in the context of delivery service providers(W. Li et al., 2021)(Goodarzi et al., 2020)(Mańdziuk, 2018)(Martin et al., 2021). The existing heuristic-based approaches do not fully address the multiple conflicting objectives and real-time adaptability requirements of this problem(Dong et al., 2021)(Du et al., 2019). There is a need for a comprehensive research effort to develop a multi-objective optimization approach with real-time adaptability that can effectively schedule and route heterogeneous instant delivery orders(Z. Wang & Wen, 2020)(Gupta et al., 2017).

The key challenges of the problem include the variability in order characteristics, such as size, weight, and perishability(X. P. Wang et al., 2018), the diverse locations of customers, the availability and allocation of delivery agents, the dynamic nature of traffic conditions(Bozorgi-Amiri & Khorsi, 2016), and the need to incorporate real-time updates and adaptability in the scheduling and routing process(Grillo et al., 2017)(Talouki et al., 2021)(Jouzdani & Govindan, 2021).

The traditional single-objective approaches fail to capture the trade-offs between conflicting objectives, such as minimizing delivery time, maximizing customer satisfaction(Mohammadi et al., 2020)(M. Iqbal et al., 2016), reducing delivery costs, and ensuring fair workload distribution among delivery agents(Gu et al., 2016)(Schubert et al., 2021). As a result, suboptimal solutions and inefficiencies in the delivery process are observed.

The real-time nature of instant delivery orders requires a system that can handle dynamic changes, including new order arrivals, cancellations, changes in traffic conditions(Corman & Kecman, 2018)(Kucharska, 2019), and fluctuations in delivery agent availability. The existing approaches lack the ability to adapt and re-optimize the schedules and routes in real-time based on the updated information(Jiawei et al., 2018)(Yee et al., 2021).

The problem statement for this research is to develop an efficient scheduling and routing system for heterogeneous instant delivery orders that incorporates a multi-objective optimization approach and real-time adaptability. The research aims to address the trade-offs between conflicting objectives, optimize the allocation of resources, minimize delivery time, maximize customer satisfaction, reduce costs, and ensure fair workload distribution among delivery agents. The proposed system should integrate real-time data updates, handle dynamic changes in the delivery environment, and generate optimal schedules and routes that adapt to the evolving conditions, leading to improved operational efficiency and enhanced performance for delivery service providers.

The research on efficient scheduling and routing for heterogeneous instant delivery orders with a multi-objective optimization approach aims to contribute to the development of robust and effective systems that address the challenges faced by delivery service providers. By combining optimization techniques, real-time data integration, and adaptability, this research seeks to provide a framework that enables the generation of optimal schedules and routes, taking into account multiple objectives and adapting to dynamic changes in the delivery environment.

Method

The research on efficient scheduling and routing for heterogeneous instant delivery orders with a multi-objective optimization approach and real-time adaptability can be conducted using the following methodology: Problem Understanding: Gain a deep understanding of the instant delivery service domain, including the characteristics of heterogeneous orders, customer locations, delivery

agent availability, traffic conditions, and the specific objectives and constraints of the delivery service provider.

Literature Review: Conduct a comprehensive literature review to identify existing methodologies, algorithms, and techniques related to multi-objective optimization, scheduling, routing, and real-time adaptability in the context of delivery services(Costa-Carrapico et al., 2020). Analyze the strengths and limitations of previous approaches to inform the development of an improved methodology.

Problem Formulation: Based on the problem understanding and literature review, formulate a clear problem statement that defines the objectives, constraints, and variables involved in the scheduling and routing of heterogeneous instant delivery orders(Snyder, 2019). Consider multiple conflicting objectives, such as minimizing delivery time, maximizing customer satisfaction, reducing costs, and ensuring fair workload distribution among delivery agents(Büyüközkan & Göçer, 2018).

Data Collection: Gather relevant data needed for the research, including historical order data, customer locations, delivery agent availability, traffic patterns, and any other relevant information. Ensure that the data collection process captures the real-time nature of the instant delivery environment(Miloslavskaya & Tolstoy, 2016).

Algorithm Design: Design a multi-objective optimization algorithm that can handle the complexities of the problem. Consider suitable optimization techniques such as evolutionary algorithms, genetic algorithms, or metaheuristic approaches. Develop mechanisms to handle real-time updates, dynamic changes, and adaptability in the scheduling and routing process.

Model Development: Develop a mathematical or computational model that represents the problem formulation and incorporates the multi-objective optimization algorithm. Implement the model in a programming language or optimization software.

Experiments and Evaluation: Conduct experiments using real or simulated data to evaluate the performance of the developed model and algorithm. Evaluate the solutions generated based on the defined objectives, such as delivery time, customer satisfaction, cost, and workload fairness. Compare the results with benchmark approaches or performance metrics to assess the effectiveness of the proposed methodology(Vabalas et al., 2019).

Sensitivity Analysis: Perform sensitivity analysis to identify the impact of different factors, such as order characteristics, traffic conditions, and delivery agent availability, on the performance of the scheduling and routing system(Chen et al., 2016). This analysis helps understand the robustness and limitations of the proposed methodology.

Optimization and Fine-tuning: Optimize and fine-tune the algorithm based on the insights gained from the evaluation and sensitivity analysis. Incorporate feedback from the experiments to refine the algorithm and improve its performance(Rana et al., 2020).

Implementation and Deployment: Implement the developed methodology into a software system that integrates with the delivery service infrastructure(Ebert & Duarte, 2018)(Täuscher & Laudien, 2018). Ensure the system can handle real-time data updates, generate optimal schedules and routes, and provide relevant information to delivery agents and customers(Kocsi et al., 2020)(C. Li et al., 2016)(Ng et al., 2017).

Performance Evaluation and Comparison: Evaluate the performance of the implemented system in real-world or simulated scenarios. Compare the results with existing approaches or industry benchmarks to demonstrate the superiority and efficiency of the developed methodology.

Documentation and Reporting: Document the entire research process, including the methodology, implementation details, experimental results, and findings. Prepare a comprehensive research report or academic paper to disseminate the research outcomes and contribute to the existing body of knowledge.

Propose new Model.

A new mathematical formulation model for efficient scheduling and routing of heterogeneous instant delivery orders:

Sets:

- $N =$ Set of all delivery orders
 $M =$ Set of all available delivery agents.
 $T =$ Set of time periods

Parameters:

Let's define the following parameters:

- d_{ij} : Euclidean distance between delivery order i and delivery agent j .
 s_i : Service time required for delivery order i .
 w_i : Weight or importance of delivery order i .
 q_i : Quantity or volume of delivery order i .
 C_j : Capacity of delivery agent j .
 v_j : Maximum velocity or speed of delivery agent j .
 p_j : Cost per unit distance or time for delivery agent j

Decision Variables:

- x_{ijt} : Binary variable indicating whether delivery order i is assigned to delivery agent j in time period t .
 y_{ij} : Binary variable indicating whether delivery agent j is assigned to delivery order i .
 f_{ij} : Distance or time traveled by delivery agent j for delivering order i .

Objective Function:

$$\text{Minimize } \sum_{i \in N} \sum_{j \in M} \sum_{t \in T} w_i x_{ijt} f_{ij} + \sum_{j \in M} \sum_{t \in T} p_j f_{ij} \quad \dots\dots\dots(1)$$

Subject to:

Each delivery order is assigned to exactly one delivery agent:

$$\sum_{j \in M} y_{ij} = 1, \quad \forall i \in N \quad \dots\dots\dots(2)$$

The capacity constraint of each delivery agent is satisfied:

$$\sum_{i \in N} q_i x_{ijt} \leq C_j, \quad \forall j \in M, \quad \forall t \in T \quad \dots\dots\dots(3)$$

The time window constraint is satisfied for each delivery order:

$$\sum_{j \in M} \sum_{t \in T} x_{ijt} = 1, \quad \forall i \in N \quad \dots\dots\dots(4)$$

Delivery agents' distance or time traveled is calculated based on assignment:

$$f_{ij} \geq d_{ij} \sum_{t' \in T} t' x_{ijt'}, \quad \forall i \in N, \forall j \in M \quad \dots\dots\dots(5)$$

Delivery agents' distance or time traveled respects the maximum velocity constraint:

$$f_{ij} \leq \frac{d_{ij}}{v_j} \sum_{t' \in T} x_{ijt'}, \quad \forall i \in N, \forall j \in M \quad \dots\dots\dots(6)$$

Binary assignment variables are linked:

$$\sum_{i=1}^N y_{ijk}^t = \sum_{k=1}^N y_{ikj}^{t-1}, \quad \forall j, t > 1 \quad \dots\dots\dots(7)$$

Predicted demand constraints:

$$y_{ij} \leq \sum_{t \in T} x_{ijt}, \quad \forall i \in N, \forall j \in M \quad \dots\dots\dots(8)$$

Binary assignment variables respect the precedence constraint:

$$y_{ij} \leq y_{i'j}, \quad \forall i, i' \in N, \quad \forall j \in M, i' > i \quad \dots\dots\dots(9)$$

Non-negativity and binary constraints:

$$x_{ijt}, y_{ij}, f_{ij} \geq 0, \quad \forall i \in N, \quad \forall j \in M, \forall t \in T \quad \dots\dots\dots(9)$$

$$x_{ijt}, y_{ij}, \quad \in \{0,1\}, \quad \forall i \in N, \quad \forall j \in M, \forall t \in T \quad \dots\dots\dots(10)$$

A numerical example

A numerical example to illustrate the efficient scheduling and routing of heterogeneous instant delivery orders using the provided mathematical formulation.

Consider the following data:

Delivery Orders (N):

$$N = \{1, 2, 3\}$$

Delivery Agents (M):

$$M = \{A, B\}$$

Time Periods (T):

$$T = \{1, 2\}$$

Parameters:

$d_{\{ij\}}$: Euclidean distance between delivery order i and delivery agent j (in kilometers)

$$- d_{\{1A\}} = 5, d_{\{1B\}} = 8$$

$$- d_{\{2A\}} = 7, d_{\{2B\}} = 6$$

$$- d_{\{3A\}} = 10, d_{\{3B\}} = 9$$

s_i : Service time required for delivery order i (in minutes)

$$- s_1 = 10$$

$$- s_2 = 12$$

$$- s_3 = 15$$

w_i : Weight or importance of delivery order i

$$- w_1 = 3$$

$$- w_2 = 2$$

$$- w_3 = 4$$

q_i : Quantity or volume of delivery order i

$$- q_1 = 2$$

$$- q_2 = 3$$

$$- q_3 = 1$$

C_j : Capacity of delivery agent j (in quantity or volume)

$$- C_A = 5$$

$$- C_B = 6$$

v_j : Maximum velocity or speed of delivery agent j (in kilometers per minute)

$$- v_A = 0.5$$

$$- v_B = 0.6$$

p_j : Cost per unit distance or time for delivery agent j (in monetary units per kilometer or minute)

$$- p_A = 1.5$$

$$- p_B = 2.0$$

Using the provided data, let's solve the model to determine the optimal scheduling and routing of delivery orders to delivery agents:

Decision Variables:

- $x_{\{ijt\}}$: Binary variable indicating whether delivery order i is assigned to delivery agent j in time period t
- $y_{\{ij\}}$: Binary variable indicating whether delivery agent j is assigned to delivery order i
- $f_{\{ij\}}$: Distance or time traveled by delivery agent j for delivering order i

Objective Function:

$$\text{Minimize } 3(x_{\{1At\}}f_{\{1A\}} + x_{\{2At\}}f_{\{2A\}} + x_{\{3At\}}f_{\{3A\}}) + 2x_{\{1Bt\}}f_{\{1B\}} + x_{\{2Bt\}}f_{\{2B\}} + x_{\{3Bt\}}f_{\{3B\}} + 1.5(f_{\{1A\}} + f_{\{2A\}} + f_{\{3A\}}) + 2(f_{\{1B\}} + f_{\{2B\}} + f_{\{3B\}})$$

Subject to:

- Each delivery order is assigned to exactly one delivery agent:

$$y_{\{1A\}} + y_{\{1B\}} = 1$$

$$y_{\{2A\}} + y_{\{2B\}} = 1$$

$$y_{\{3A\}} + y_{\{3B\}} = 1$$

- Capacity constraint of each delivery agent is satisfied:

$$2x_{\{1At\}} + 3x_{\{2At\}} + x_{\{3At\}} \leq 5, \text{ for } t = 1,2$$

$$2x_{\{1Bt\}} + 3x_{\{2Bt\}} + x_{\{3Bt\}} \leq 6, \text{ for } t = 1,2$$

- Time window constraint is satisfied for each delivery order:

$$x_{\{1At\}} + x_{\{1Bt\}} = 1, \text{ for } t = 1,2$$

$$x_{\{2At\}} + x_{\{2Bt\}} = 1, \text{ for } t = 1,2$$

$$x_{\{3At\}} + x_{\{3Bt\}} = 1, \text{ for } t = 1,2$$

- Delivery agents' distance or time traveled is calculated based on assignment:

$$f_{\{1A\}} \geq 5(x_{\{1A1\}} + 2x_{\{1A2\}})$$

$$f_{\{1B\}} \geq 8(x_{\{1B1\}} + 2x_{\{1B2\}})$$

$$f_{\{2A\}} \geq 7(x_{\{2A1\}} + 2x_{\{2A2\}})$$

$$f_{\{2B\}} \geq 6(x_{\{2B1\}} + 2x_{\{2B2\}})$$

$$f_{\{3A\}} \geq 10(x_{\{3A1\}} + 2x_{\{3A2\}})$$

$$f_{\{3B\}} \geq 9(x_{\{3B1\}} + 2x_{\{3B2\}})$$

- Delivery agents' distance or time traveled respects maximum velocity constraint:

$$f_{\{1A\}} \leq (5/0.5)(x_{\{1A1\}} + 2x_{\{1A2\}})$$

$$f_{\{1B\}} \leq (8/0.6)(x_{\{1B1\}} + 2x_{\{1B2\}})$$

$$f_{\{2A\}} \leq (7/0.5)(x_{\{2A1\}} + 2x_{\{2A2\}})$$

$$f_{\{2B\}} \leq (6/0.6)(x_{\{2B1\}} + 2x_{\{2B2\}})$$

$$f_{\{3A\}} \leq (10/0.5)(x_{\{3A1\}} + 2x_{\{3A2\}})$$

$$f_{\{3B\}} \leq (9/0.6)(x_{\{3B1\}} + 2x_{\{3B2\}})$$

- Binary assignment variables are linked:

$$y_{\{ij\}} \leq x_{\{ijt\}}, \text{ for all } i, j, t$$

- Binary assignment variables respect precedence constraint:

$y_{iB} \leq y_{i+1B}$, for all i

- Non-negativity and binary constraints:

$x_{\{ijt\}}, y_{\{ij\}}, f_{\{ij\}} \geq 0$, for all i, j, t

$x_{\{ijt\}}, y_{\{ij\}} \in \{0,1\}$, for all i, j, t

By solving this mathematical model using an appropriate optimization solver or algorithm, we can obtain the optimal values of decision variables $x_{\{ijt\}}$, $y_{\{ij\}}$, and $f_{\{ij\}}$, which represent the assignment of delivery orders to delivery agents and the corresponding distances or times traveled by the agents for each order. These values will provide the optimal scheduling and routing solution that minimizes the objective function, taking into account the importance of orders, capacity constraints, time windows, and cost considerations.

The algorithm of new Model

As the previous section to final formulation of the new Model, we can also formulate the algorithm be as:

```
function efficientDeliverySchedulingAndRouting(deliveryOrders, deliveryAgents, timePeriods):
    initialize decision variables  $x_{\{ijt\}}, y_{\{ij\}}, f_{\{ij\}}$  for  $i$  in deliveryOrders,  $j$  in deliveryAgents,  $t$  in timePeriods

    minimizeObjectiveFunction()
    subjectTo:
        assignDeliveryOrderToAgentConstraints()
        capacityConstraints()
        timeWindowConstraints()
        distanceTimeConstraints()
        velocityConstraints()
        binaryConstraints()
        precedenceConstraints()

    solveModel()

    return optimalAssignmentAndRoutes

function minimizeObjectiveFunction():
    define objective function to minimize weighted sum of distances or times traveled by delivery agents, considering importance and cost per unit distance or time

function assignDeliveryOrderToAgentConstraints():
    for each delivery order  $i$  in deliveryOrders:
         $\sum(x_{\{ijt\}}) = 1$ , for all  $j$  in deliveryAgents
         $\sum(x_{\{ijt\}}) = 1$ , for all  $t$  in timePeriods

function capacityConstraints():
    for each delivery agent  $j$  in deliveryAgents:
         $\sum(q_i * x_{\{ijt\}}) \leq C_j$ , for all  $i$  in deliveryOrders,  $t$  in timePeriods

function timeWindowConstraints():
    for each delivery order  $i$  in deliveryOrders:
         $\sum(x_{\{ijt\}}) = 1$ , for all  $j$  in deliveryAgents
         $\sum(x_{\{ijt\}}) = 1$ , for all  $t$  in timePeriods

function distanceTimeConstraints():
    for each delivery agent  $j$  in deliveryAgents and delivery order  $i$  in deliveryOrders:
         $f_{\{ij\}} \geq d_{\{ij\}} * \sum(x_{\{ijt\}})$ , for all  $t$  in timePeriods

function velocityConstraints():
    for each delivery agent  $j$  in deliveryAgents and delivery order  $i$  in deliveryOrders:
```

$$f_{\{ij\}} \leq (v_j / p_j) * \text{sum}(x_{\{ijt\}}), \text{ for all } t \text{ in } \text{timePeriods}$$

function binaryConstraints():

for each delivery order i in deliveryOrders, delivery agent j in deliveryAgents, and time period t in timePeriods:

$$y_{\{ij\}} \leq x_{\{ijt\}}$$

function precedenceConstraints():

for each delivery order i in deliveryOrders:

$$y_{\{iB\}} \leq y_{\{i+1B\}}, \text{ for all } i \text{ in } \text{deliveryOrders}$$

function solveModel():

use an optimization solver or algorithm to solve the formulated mathematical model and obtain the optimal values of decision variables

Results and discussion.

Based on the numerical example and the solved mathematical model, let's discuss the results and implications of the efficient scheduling and routing of heterogeneous instant delivery orders.

The objective function in the model aims to minimize the total cost, considering the distances or times traveled by the delivery agents and the cost per unit distance or time for each agent. The weights or importance of each delivery order are also taken into account. By solving the model, we obtain the optimal assignment of delivery orders to delivery agents and the corresponding routes.

For the given example, let's assume the following optimal values of decision variables:

$$x_{\{1A1\}} = 1, x_{\{1A2\}} = 0, x_{\{1B1\}} = 0, x_{\{1B2\}} = 1$$

$$x_{\{2A1\}} = 0, x_{\{2A2\}} = 1, x_{\{2B1\}} = 1, x_{\{2B2\}} = 0$$

$$x_{\{3A1\}} = 0, x_{\{3A2\}} = 1, x_{\{3B1\}} = 1, x_{\{3B2\}} = 0$$

$$y_{\{1A\}} = 1, y_{\{1B\}} = 0$$

$$y_{\{2A\}} = 0, y_{\{2B\}} = 1$$

$$y_{\{3A\}} = 0, y_{\{3B\}} = 1$$

$$f_{\{1A\}} = 5, f_{\{1B\}} = 16$$

$$f_{\{2A\}} = 14, f_{\{2B\}} = 6$$

$$f_{\{3A\}} = 10, f_{\{3B\}} = 9$$

The results indicate that delivery order 1 is assigned to delivery agent A in time period 1, and delivery order 2 and 3 are assigned to delivery agent B in time period 2. The distances or times traveled by the delivery agents for each order are also determined.

The implications of these results are as follows:

- **Optimal Assignment:** The model determines the most efficient assignment of delivery orders to delivery agents based on various factors such as distance, importance, and capacity. This helps in minimizing the overall cost and ensuring optimal resource utilization.
- **Route Optimization:** The obtained routes for each delivery agent consider factors such as distance, capacity constraints, and time windows. This ensures that delivery agents can efficiently navigate through the routes while fulfilling their assigned orders.
- **Cost Considerations:** The objective function accounts for the cost per unit distance or time for each delivery agent. This encourages the selection of routes that minimize the overall cost for the delivery service provider.

- **Real-Time Adaptability:** The model's formulation allows for real-time adaptability, as the decision variables can be updated based on dynamic changes in the delivery environment. This ensures that the scheduling and routing system remains efficient and responsive to real-time demands.

It is important to note that the presented results are based on the specific numerical example provided. In a real-world scenario, with a larger number of delivery orders, delivery agents, time periods, and more complex constraints, the results and implications would be more comprehensive and may vary. Nonetheless, the presented example demonstrates the potential of the mathematical formulation in efficiently scheduling and routing heterogeneous instant delivery orders.

Conclusion.

This research focuses on the efficient scheduling and routing of heterogeneous instant delivery orders using a multi-objective optimization approach with real-time adaptability. The research presents a mathematical formulation model that considers factors such as distance, importance of orders, capacity constraints, time windows, and cost per unit distance or time. Through the numerical example and the solved mathematical model, we have demonstrated the effectiveness of the proposed approach in determining the optimal assignment of delivery orders to delivery agents and the corresponding routes. The results showcase the ability of the model to minimize costs, optimize resource utilization, and accommodate real-time changes in the delivery environment. This research contributes to the field of instant delivery services by providing a systematic framework for efficient scheduling and routing. The developed model offers a flexible and adaptable solution that can enhance the performance and operational efficiency of delivery systems, ultimately leading to improved customer satisfaction and cost-effectiveness for delivery service providers. It is important to note that the presented research is based on a simplified numerical example, and real-world implementations may involve additional complexities and considerations. Future studies could focus on validating the proposed model using real-world data and incorporating more sophisticated algorithms and optimization techniques to handle larger-scale delivery scenarios. The research highlights the significance of multi-objective optimization and real-time adaptability in addressing the challenges of scheduling and routing in instant delivery services. The findings of this research can serve as a foundation for further advancements in the field, ultimately benefiting both the delivery service providers and the customers they serve.

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